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NAVY UNDERWATER SOUND LAB NEW LONDON CONN
A COMPUTER PROGRAM TO CALCULATE NORMAL MODE PROPAGATION OVER A --ETC(U)

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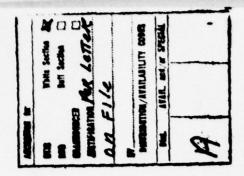
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LEVEL II OUN LIBRARY COPY MOST ProJect Copy No. Code No. NUSL Problem No. 0-A-409-00-00 SF 11 552 001-14054 24 000 NAVY UNDERWATER SOUND LABORATORY NEW LONDON, CONNECTICUT 06320 A COMPUTER PROGRAM TO CALCULATE NORMAL MODE PROPAGATION OVER A FLAT HOMOGENEOUS OCEAN BOTTOM AD AO 66654 bу 1979 William G. Kanabis NUSL-TM-NUSL Technical Memorandum N 2211-296-69 13 October 1969 INTRODUCTION This memorandum describes NUSL Program S1441 written in FORTRAN V. This program uses normal mode theory to predict acoustic propagation over a flat homogeneous ocean bottom. Program S1441 is an extension of a program written for NUSL by A.D. Little Inc. (Reference 1 and 2). In the A.D. Little program the amplitude distribution of an acoustic signal as a function of depth is determined for a given mode by means of the numerical solution of the acoustic wave equation for given boundary conditions. Program S1441 calculates and produces Calcomp plots of the following for any mode. frequency and velocity profile: Amplitude as a function of depth and the ray equivalent of any mode. b. Group velocity, phase velocity, excitation pressure, and angle of incidence of sound waves striking the boundaries. c. Propagation loss as a function of range. DISTRIBUTION STATEMENT A Approved for public release; Distribution Unlimited



NORMAL MODE THEORY

Normal mode theory is based on the assumption that at large distances from a source standing waves formed by energy striking the boundaries in certain preferred directions form the main part of the sound field.

Solution of Wave Equation

There are three methods by which these preferred directions and the amplitude distribution of the standing waves may be determined. First one may find the solution in closed form of the wave equation.

$$\Delta_{3} \dot{\Phi} = \frac{C_{3}}{7} \frac{2 f_{3}}{9_{3} \dot{\Phi}} \tag{1}$$

Where Φ is a displacement or velocity potential and C is the velocity of sound in the medium considered. This is done in Reference 3 by integrating equation (1) subject to the boundary conditions in the complex plane and approximating the normal mode solution for the standing waves by the evaluation obtained from the residues in the integration.

A second method is the solution of equation (1) by direct numerical integration. This was done by A.D. Little Inc by means of a computer program described in References 1 and 2.

Third it has been shown in Reference 4 that one may consider the ray paths, which undergo total reflection at the boundaries and whose successive upgoing and downing rays are in phase, as the descriptions of the modes.

A. Numerical Integration of the Wave Equation

The basis of this program is the direct numerical integration of the wave equation. This method which is extremely well suited for analysis by means of a high speed computer is discussed below.

When equation (1) is solved for Φ the incremental pressure p is found by definition

$$b = -b \frac{2\epsilon_1}{2}$$
 (5)

Where Φ is the displacement potential

ho is the material density at the point considered

It is found that equation (1) is separable in terms of range r and depth **2** so that the pressure amplitude can be written as

$$p_{i} = F(r) \cdot u(z) \tag{3}$$

and a differential equation in terms of Pa may be obtained.

$$\frac{d^{2}y}{dz^{2}} + \left(\frac{y}{c^{2}} - k_{r}^{2}\right)y = 0$$
 (4)

where w = the radial frequency

c = sound velocity

u = u(z) is the pressure amplitude distribution as a function of depth

k = horizontal wave number

where Θ is measured relative to the normal to the ocean bottom.

The physical picture presented by equation (3) is that of a standing wave with a particular pressure amplitude distribution as a function of depth, u(a), which travels unchanged in shape as it progresses in the r direction.

Equation (4) may be written as

$$\frac{d^2u}{d^2u} + f(z)u = 0 \tag{6}$$

where

$$5(2) = \frac{\omega^2}{2} - k^2$$
 (7)

In solving equation (4) there are three constraints which must be imposed upon any solution. These constraints are due to boundary conditions at the interface between the water and bottom material and at the waters surface.

First due to the necessity of continuity of pressure and particle velocity in the vertical direction at the bottom interface, it is necessary that

$$\frac{1}{u_1} \frac{du_1}{dz} \cdot \frac{p_1}{p_2} \sqrt{k_r^2 - \frac{w^2}{c_2^2}}$$
 (8a)

where the terms having subscript b refer to these quantities in the bottom material on one side of the interface while those with subscript 1 refer to the water side of the interface.

Second, since we assume a pressure release surface at the air-water boundary then

at this surface.

Third, the modes by definition involve propagation with energy which strikes the bottom at angles larger than the critical angle so that "total reflection" occurs. Since the critical angle Q measured relative sin Oc = Si to the normal to the interface is given by

(naturally C must be creater than C,)

then

must hold for all energy striking the bottom.

Since

using euation (7) and the condition of continuity of pressure we obtain the result that

$$|\xi(z)| < \frac{\omega^2}{\omega^2} - \frac{\omega^2}{\omega^2}$$
 (8c)

at the bottom interface.

Upon examining equation (6) it can be seen that a solution of the equation is of the form

U(3) = Be (3(3) 3

for given values of sow and k. . B is a constant. If s(2) is positive (2) is in the form of a sinosoid. This kind of solution is obtained for the interference pattern between upgoing and downgoing waves in the water. If (2) is negative w(2) is in the form of an exponential. 5(1) is negative for the following two cases. It is negative everywhere in the bottom and it is negative in the water at depths which correspond to shadow zones caused by vertexing of rays which form a mode. Both distributions are a result of the condition of continuity of pressure in the medium. Thus when there is "total reflection" at a level either by vertexing or reflection from a boundary and the pressure is finite at that level then at adjacent levels there may be a decay (whose rate is determined by the boundary conditions), but not a discontinuous step to zero pressure. An example of a distribution involving both exponentials is shown in Figure 1 which shows the amplitude distribution as a function of depth and Figure 2 which shows the ray equivalent of the mode. In Figure 2 it is seen that the ray equivalent of the normal mode vertexes at a depth of 48 feet. Therefore, in Figure 1 the pressure amplitude distribution is in the form of an exponential between the surface of the ocean and a depth of 48 feet. It can also be seen in Figure 1 that the pressure amplitude distribution in the bottom is in the form of an exponential.

In order to integrate equation (6) numerically formulas relating Un., and its derivative Un, with the quantities Un and Un must be obtained (The subscripts signify the depth at which they are calculated). This is done by writing a Taylor series for Un, and Un... The details of this procedure is given in References 1 and 2. The results are summarized in equations (9) and (10)

where

h is the increment between level n and level no.

In and Invare the values of (1) at m and man.

Equations (9) and (10) are recursion relationships such that given values for \mathbf{u}_i and \mathbf{u}_i' which are the values of \mathbf{u}_i and \mathbf{u}_i' just above the bottom we can calculate \mathbf{u}_i and \mathbf{u}_i' at all levels in the water.

Since we are interested in normalized values of we over the water column we can select who to be any arbitrary value (which is convenient). For an arbitrary value of the horizontal wave number k, which is restricted by equation (8c) we can evaluate who by equation (8a). Then we can determine u for all levels by using equations (9) and (10) repeatedly. If the value of k, corresponds to a mode, equation (8b) will be

satisfied at the surface of the water. Each mode has at most one such solution for a given frequency. There is a low cut-off frequency for each mode so that at frequencies below the cut-off frequency equation (8b) cannot be satisfied.

After finding the amplitude distribution of a mode it is necessary to define the mode number. For a finite frequency the mode number is equal to the number of nodes in the amplitude distribution. Thus, the first mode has a node only at the surface. A representation of the amplitude distribution of the first mode is shown in Figure 1.

B. Ray Equivalent

Corresponding to the definition of a mode discussed above is a more physical approach in which the ray equivalent of the solution to the wave equation is considered. This approach has been discussed previously, References 5 and 6, and in Reference 7.

For simplicity let us consider a two layer medium of constant water depth H, density A, and sound velocity C, lying over a infinite bottom of density A and sound velocity C, as shown in Figure 3. At large ranges from a point source we may consider sound to be propagated by plane waves. It is clear from Figure 3 that for certain waves whose direction is defined by an angle O there will be constructive interference between it and a plane wave which undergoes one more bottom and surface reflections. In order for constructive interference to exist the phase difference between points A and B, Figure 3 must be 2(n-1) m degrees, or it must satisfy the equation:

$$\frac{3\pi}{2\pi} \left[\frac{H}{Coc\theta} + \frac{H}{Coc\theta} \cos 2\theta \right] - E - \pi = 2(N-1)\pi$$

or

$$\frac{\lambda_m}{\lambda_m} \left[\lambda H \cos \Theta \right] - \varepsilon - \pi + \lambda (N-1) \pi \tag{11}$$

where λ_n is the wavelength of the preferred mode, ϵ is the phase change undergone by a plane wave upon bottom reflection, n is the mode number, and the phase change upon reflection from the water surface is assumed to be $-\pi$. If the sound velocity in the water layer varies with depth the first term of equation (11) would be different from that given above. However, the discussion below applies to either case.

If for a given wavelength λ_n and angle Θ there is constructive interference between plane waves suffering different numbers of bottom

and surface reflections, then propagation consists of a series of upgoing and downgoing waves as shown in Figure 4. The left hand term of equation (11) is the phase change, 2Δ , undergone in the Z direction when a ray makes a surface-bottom-surface cycle. For finite frequencies

as

Therefore, the phase change, \triangle , undergone in the 2 direction over the water depth is limited by the following

The pressure is zero at the surface, the phase change upon reflection is $\neg \pi$, and the direction of propagation is reversed upon reflection from the surface. Therefore, the sound field in the vertical direction is the sum of two sine waves, representing the upgoing and downgoing waves in the 2 direction. These waves are shown for the first two modes in Figure 5. Because of equation (12) the number of nodes in this amplitude distribution is equal to the mode number. Thus there is a correspondence between the definitions of mode number in the solution of the wave equation and the ray equivalent solution.

When the wave equation is solved numerically values of (1) are obtained. 5(2) is given in equation (7) by

$$f(2) = \frac{4k^2}{2} - k_1^2$$
 (13)

where k- is given in equation (5) by

Therefore given positive **Ma** one can determine from equations (13) and (14) the cosine of the angle of inclination of the equivalent ray

as a function of 2.

If the ray between two points 2, and 2, is continuous then $\triangle 2 \cdot 2 \cdot 2$, may be given in terms of the horizontal distance $\triangle R \cdot R \cdot R$, and one particular value of the tan 3 over the path. This relationship is

where con the vertex velocity = constant

If the value of & does not vary appreciably between 1 and 1 then we can approximate tand by

ton 8. ton 8. t ton 0.

where & and O, are taken at 1.1, and L respectively. (Reference 8)

$$\frac{\Delta R}{\Delta z} \approx \frac{1}{C_V} \frac{C_1 + C_2}{\cos \theta_1} \qquad (16)$$

Cy = vertex velocity

c,, <= are the sound velocity at 1 and 12 A, 0, = angle relative to normal of ray at 3,

Thus given values of &(a) one can construct a ray equivalent. If vertexing takes place the depth L at which this occurs is the level whose value of sound velocity equals C. .

C. Phase Velocity and Group Velocity

The phase velocity V_p is given by the relationship

where Θ is the direction of propagation of a plane wave where the sound velocity has a value C. Equation (17) can also be written

where C, is the vertex velocity

The group velocity can be considered from two points of view. First group velocity V3 may be considered as a measure of the speed of propagation in the horizontal direction of a number of frequencies in a band and centered about w . Vg may be given by (Reference 9)

$$V_{9} = \frac{\Delta \omega}{\Delta k}$$
 (19)

or by (Reference 10)

$$\frac{V_0}{c} = \frac{V_p}{c} + (kH) \frac{d(\frac{V_p}{c})}{d(kH)}$$
 (20)

It can be seen that this approach to the calculation of group velocities involves the calculation of derivatives. This is not desirable in a computer program since this produces inaccuracies and makes it necessary to obtain an unnecessarily large number of values of group velocity as a function of frequency.

Tolstoy (Reference 11) has used a general theorem by Biot (Reference 12) to show the equivalence of N_3 in equations 19 and 20 to the rate of energy transport in the horizontal direction. The group velocity is given by

$$V_9 \cdot \frac{1}{V_p} \frac{v}{\sigma}$$
 (21)

where

where ρ and c are respectively the density and sound velocity at c, and c is given in the equation

$$\Phi = \Phi(\pm)e^{i(\pm dx - \omega + 1)} \tag{24}$$

where Φ is the displacement potential in equation (1).

Since by equation (2)

$$P = -\beta \frac{\partial + f}{\partial x^2}$$
 (2)

and u is the value of pressure, normalized to maximum amplitude, as a function of \mathbf{z} then by equations (2) and (24)

where ψ is the normalized value of ϕ .

Thus by (25) we can obtain ψ once ω is known since we are only interested in the normalized values of ω and ψ for given ω .

Given ρ , in the water and ρ in the bottom and α normalized to maximum pressure amplitude, in order to obtain α , the normalization of

where I and be signify water and bottom and use signifies unnormalized. Since the maximum value of use lies in the water, since A is greater than A, and because (1) is normalized with respect to maximum amplitude we multiply both expressions in (25a) by p, to obtain o normalized with respect to maximum amplitude so that

$$\varphi_{b} = \mathcal{U}(\mathbf{z}) \qquad (25b)$$

is the normalized value for ϕ and may be used in place of ϕ in equations (21-23).

D. Excitation Pressure and Propagation Loss

The sound field produced by a simple harmonic source in a two-layered half-space (shown in Figure 6) with a free surface at 2.0 and the boundary between two fluids at 2. h is given by the solution of equation (1). This is given in Reference (9) by

where

r = horizontal range

w = radial frequency

w = mode number

= horizontal wave number k for mode m

where A is the water density at the source

Qualis the normalized displacement potential, a function of

is the source depth

is the receiver depth is the mode number

pm is the excitation function given by

where P is the water density

c. is sound velocity at the source

S is the power output of an omnidirectional source

is the horizontal wave number

and

where on is the normalized displacement potential.

If the source produces a unit sound pressure level then the following relationship (Reference 9) must be satisfied

$$4\pi \left(\frac{Sc_0\rho_0}{2\pi}\right)^{12} = 1 \tag{30}$$

Substituting (30) into equation (28) we obtain the exitation pressure R such that

$$P_{m} = \frac{P_{n}(2\pi)^{1/2}}{2U_{m}(\kappa_{m})}$$

$$(31)$$

The exitation pressure is the sound pressure amplitude produced by a source which generates a unit source pressure level at unit range when both source and receiver are at antinodes. It is essentially a measure of the source level of mode m for a unit source.

From equation (26) we determine the pressure amplitude characteristics of the sound field and this amplitude, p., is given by

Since pa is the sound pressure amplitude at range r from a generator with unit source level, the value of propagation loss r at range r for a given depth of source and receiver is given by

It can be seen from equations (27) and (32) that once wis known one can easily determine the effect of the source and receiver depth on the sound field at a given range. If the source depth is such that while, where is the source depth, is a node the mode we will

¹The quantity is represented by the symbol of capital W in Reference 9.

be suppressed in the sound field. Likewise, if L is such that $Q_m(L)$ is an antinode the sound field of mode m will be greater than at any depth for which Q(L) is less than $Q_m(L)$. The preceding also applies to a discussion of the effect of the receiver depth upon the sound field.

It can also be seen from equations (27), (28), and (29) that the pressure amplitude determined does not depend upon the normalization of $\phi(\lambda)$.

For small attenuation of individual modes equation (32) may be rewritten to include losses at the boundaries as a function of range D_m for mode m so that

where Pm is given in db of loss per unit increment in range.

DESCRIPTION OF PROGRAM S1441

Program S1441 uses normal mode theory to predict acoustic propagation over a flat homogeneous ocean bottom. The program may be used with any of three options, each of which provides different information about the sound field in a medium for a given frequency, velocity profile, and mode number.

The three options provide as output the following calcomp plots:

- A. The first option produces two plots for each mode analyzed. One plot gives pressure normalized to the maximum amplitude as a function of depth. Another plot gives the ray equivalent of the mode.
- B. The second option produces two plots for each mode. One plot gives three quantities: phase velocity, group velocity, and excitation pressure. These quantities are plotted as a function of frequency. Another plot gives the angle of incidence of energy at the two boundaries for the given modes. These angles are plotted as a function of frequency.
- C. The third option produces a plot of propagation loss versus range for any combination of modes. These plots can be produced for any source or receiver depth or frequency.

For any of the three options used, two plots of the velocity profile, shown in Figures 7 and 8, are produced. The first plot (Figure 7) shows the sound velocity in both the water and the bottom. The second plot (Figure 8) shows in more detail via an expanded velocity scale the sound velocity in the water.

The format of the input data is shown in Tables I to IX. In Table II it is shown how to obtain either of options A, B, or C. The mechanics of the individual options are described below.

Option A

In option A the numerical solution to equation (4) or (6) is found subject to the boundary conditions given by equations (8a), (8b), and (8c). Then the ray equivalent of this solution is obtained.

For a given velocity profile inputed (Table IV) the sound velocity is calculated at N (Table V) levels equispaced between the surface and bottom by interpolation between the values given.

The value of the horizontal wave number k, is varied subject to the restrictions given in equation (8c) and for each value of k, wa is calculated over the water column of N equispaced levels by means of equations (9) and (10). The values of was is restricted such that was never exceeds u, (Table V). Mode M must have M zero crossings. After was is calculated for a given k, k, is incremented by Dka so as to obtain the smallest possible value of wat the surface.

If the conditions necessary for the existence of a given mode cannot be met, the statement "No Mode Found" is printed out.

Once (12) has been found for a given mode the ray equivalent can be found by equation (16). Sample calcomp plots of the amplitude distribution normalized to maximum amplitude and ray equivalent are found in Figures 1 and 2.

For a large negative velocity gradient high frequency sound is trapped near the oceans bottom. Under these circumstances, it is difficult to obtain a good approximation to the boundary condition at the surface. Then it is necessary to decrese the value by which is incremented. This is done by using a large value (up to about 10) of IEX (Table II). A large value of IEX will increase the program time since it decreases the increment of key by a factor of 10-IEX. Under most circumstances, a value of IEX of zero is adequate.

Option B

In option B group velocity, phase velocity, excitation pressure, and angle of incidence at the boundaries relative to the normal to the boundary are found over any frequency range (Table VI). For a given frequency, group velocity is determined by equations (21), (22), and (23); phase velocity by equation (18), and excitation pressure by equation (31). The angle of incidence at the boundaries is given by equation (15). If the ray vertexes before striking a boundary, the angle of incidence is given as 90°. Sample plots obtained from Option B are shown in Figures 9 and 10.

Option C

In Option C propagation loss for a source level at a one yard reference is obtained as a function of range for any given frequency and combination of modes. Propagation loss may be calculated by equations (32) and (33). The ranges over which loss is plotted and source and receiver depth are inputed by a card described in Table VII. Values of D_{m} are inputed as shown in Table VIII and the modes which make up the sound field are inputted as shown in Table IX. A sample calcomp plot is shown in Figure 11.

CONCLUSIONS

Program S1441 is designed to calculate and plot many quantities of interest in the study of a sound field in an ocean bounded by flat parallel boundaries. The problem of acoustic propagation is approached from the standpoint both of physical and ray acoustics.

It is possible at high frequencies when the velocity profile has more than one "channel" to obtain solutions of the differential equation (6) which are physically unrealizable. This can only be detected by observing the values of (2) which are shown in the printout from this program. If two depths which have positive values of (2) which indicate propagation of rays are separated by negative values of (2) which indicate a "shadow zone" one has a physically unrealizable situation. Since the velocity profiles — taken over the BIFI range show in general a monotonically decreasing or increasing sound velocity with depth this limitable does not severely handicap analysis. However, caution should be taken in analysis when complex velocity gradients are used.

WILLIAM G. KANABIS

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FORMAT (20A4)

HEADING ON EACH PAGE OF THE OUTPUT

TABLE I

Heading Card

CARD 1

	FORMAT (I10,	F10.0, 4I10)
INPUT PARAMETER	COLUMNS	
NUMV	1-10	Number of velocities in profile
VEL 1	11-20	Velocity at origin of calcomp plot of velocity profile
IVØP	21-30	If IRP = 0 When IVOP = 0 Option A When IVOP = 1 Option B
IRP	31-40	When IVOP = 1 If IRP = 1 Option C
IVRP	41-50	<pre>IVRP = 1 Velocity profile not</pre>
IEX	51-60	IEX changes increment of Kr by a factor of 10-IEX. Values from 0-10.

TABLE II

CARD II

FORMAT (5F10.3)

INPUT PARAMETER	COLUMNS	
ZM	1-10	Water depth (ft)
СВ	11-20	Velocity of sound in the bottom (ft/sec)
RO	21-30	Density of water (grams 1 cm ³)
RB	31-40	Density of Bottom (grams 1 cm ³)
FSC	41-50	Maximum Depth Plotted in velocity profiles and plots in option A is 200 FSC

TABLE III

CARD 3

	FURMA	1 (2110.3)
INPUT PARAMETER	COLUMNS	
Z(I)	1-10	Height above bottom at which sound velocity is $C(I)$
c(I)	11-20	Velocity of sound in (ft/sec) at Z(I)

I = 1, NUMV in order of increasing Z

TABLE IV

GROUP 4 NUMV Cards

FORMAT (I10, 2F10.3)

INPUT PARAMETER	COLUMNS	
N	1-10	Number of intervals into which depth is to be sub-divided in integration of differential equations
UM	11-20	Maximum value of $u(z)$
FQ	21-30	Frequency (Hz)

TABLE V

CARD 5

	FORMAT	(4110)
INPUT PARAMETER	COLUMNS	
ISFQ	1-10	Highest frequency to be analyzed
IEFQ	11-20	Lowest frequency to be analyzed
NMOD	21-30	Number of modes analyzed Mode numbers analyzed = 1, NMOD
INCF	31-40	Decrement in frequency from ISFQ to IEFO

Options A and C ISFQ = IEFQ = FQ Option B Range of frequencies is selected by ISFQ, IEFQ, INCF

TABLE VI

CARD 6

FORMAT (4110, 3F10.3)

INPUT PARAMETER	COLUMNS	
IRST	1-10	Lowest range in feet at which propagation loss versus range will be plotted
IREN	11-20	Largest range in feet at which propagation loss will be plotted
IRIC	21-30	Increment in range to be plotted in feet
NPS	31-40	Number of propagation loss versus range plots
ZS	41-50	Source depth in feet
ZRC	51-60	Receiver in depth in feet
FMI	61-70	Increment of range on the calcomp plot per division in nautical miles

TABLE VII

CARD 7 For Option C

FORMAT (4F10.5)		
INPUT PARAMETER	COLUMNS	
DD(J) 1-	1-10	DD(J) is the loss at boundaries as a function of range in db per foot for the mode J.
	11-20	101 one mode v.
	21-30	J = 1, NMOD where NMOD is the number of modes analyzed
	31-40	

The number of cards in this group is the integer greater than or equal to the quantity $\underline{\text{NMOD}}_{\ell}$

TABLE VIII

GROUP 8 For Option C

	Card	a.
INPUT	FORMAT	110
PARAMETER	COLUMNS	
NMS	1-10	Number of modes to be summed in the plot of propagation less versus range(NM4NMOD)

Card(s) b.

FORMAT 6110

INPUT PARAMETER	COLUMNS	
MDS(J)	1-10	J = 1, NMS The value of MDS(J) are the
	11-20	mode numbers of the modes to be
	21-30	summed in the propagation loss versus range plots. MDS(J)4NMOD
	31-40	MD2 (1) S MMOD
	41-50	
	51-60	

Number of card(s) b. is the integer greater than or equal to $\frac{NMS}{6}$ Cards a and b form a set. There is a set of cards for each plot in Option C. (NPS sets)

TABLE IX

GROUP 9 For Option C

```
DOUBLE PRECISION
                         F.U.UP
    DOUBLE PRECISION
                                 K2.
                                         W2, P2, H, ZP,
                                                     CZ.G.H2.DEN
    DOUBLE PRECISION S.K20.DK2.GAM.BA
    DOUBLE PRECISION E.V
    DOUBLE PRECISION UMAX
    DOUBLE PRECISION COS2 , CCC , CV
    DIMENSION HED(20),2(100),C(100),F(500),UP(500),U(500),
      ZMP(1000), XMP(1000), COS2(500), CCC(500)
      , ZZP(500) , ZPP(500), VV(500), DATA(1024) , UU(500)
      ,PM(5000)
                        .DDT (100)
      , ZR(500) , CR(500) , RP(100) , ZBT(5) , ZBF(5)
   1,DD(100),PPT(1000),PCT(1000),PST(1000),MDS(100),USR(100),URR(100),
   1 PMM(100),FMR(100) ,FDS(100)
   1 ,GVEL(4000), PVEL(4000), FQP(4000), T1(4000), T2(4000)
    COMMON MS, JM . U
    COMMON JMS
    CALL PLOTS ( DATA(1), 1024, 6 )
  4 JPM = 25
    READ (3,1) HED
  1 FORMAT (2044)
    READ (3,112)
                        NUMV, VEL1 , IVOP , IRP , IVPL , IEX
112 FORMAT ( 110,F10.0,4110)
    NUM =
    READ(3,2) ZM,CB,RO,RB ,FSC
  2 FORMAT (5F10.3)
    ZMB = (200.0*FSC -ZM)/(20.0*FSC)
    ZBT(1) = ZM
    ZBT(2) = ZM
    ZBT(3) = 200.0 *FSC
    ZBT(4) = -20.0*FSC
    ZBF (1) = 0.0
    ZBF(2) = 10.0
    ZBF(3) = 0.0
    ZBF (4) = 1.0
    DO 3 I=1,100
    2(1) = 0.
  3 C(1) = 0.
    1=1
  5 READ (3,30) Z(1),C(1)
 30 FORMAT (2F10.3)
    IF (DABS(Z(1)-ZM)-.01)6,6,7
  7I = I+1
    GO TO 5
  6 I = 1
    IF (IVPL.EQ.1) GO TO 8
    DO 130 K = 1, NUMY CK(NUMY -K +1) = C(K)
130 ZR(NUMV -K +1) = Z(K)
    ZR(NUMV +1) = ZM -0.01
    ZR(NUMV +2) = ZM +50.0
    CR (NUMV
            +1) = CB
            +2) = Cb
    CR (NUMV
             NINY = 1, NUMV
    DO 185
                ZM - ZR(NINY)
165 ZR(NINY)
    ZR(NUMV +3) = 200.0*FSC
    ZR(NUMV +4) = -20.0+F5C
    CR (NUMV
            +3) =
                     VEL1
    CR(NUMV +4) = 50.0
```

```
CALL PLOT (0.0.0.0.-3)
    CALL LINE (CR. ZR. NUMV +2, 1,0,0 )
    CALL LINE (28F, 28T, 2, 1, 0, 0)
    CALL SYMBOL (10,25, ZMB, 0,14, 6HBOTTOM, 0,0,6)
   CALL AXIS (0.0.0.0,14HSOUND VELOCITY,14,10..0.0.CR(NUMV +3) .
   1CR(NUMV+4),10.0
    CALL AXIS (0.0,0.0,11HWATER DEPTH,11,10.0,90.0,ZR(NUMV +3) ,
   1ZR(NUMV+4),10.0
    CALL PLOT (15.0,0.0,-3)
    ZR(NUMV +1) = 200.0*FSC
    ZR(NUMV +2) = -20.0*FSC
    CR(NUMV +1) =VEL1
    CR(NUMV +2) =10.0
    CALL LINE (CR. ZR. NUMV. 1.0.0)
    CALL LINE (ZBF, ZBT, 2, 1, 0, 0)
    CALL SYMBOL (10.25, ZMB, 0.14, 6HBOTTOM, 0.0,6)
    CALL AXIS (0.0.0.0,14HSOUND VELOCITY,14,10.,0.0,CR(NUMV +1) .
   1CR(NUMV+2),10.0
    CALL AXIS (0.0,0,0,11HWATER DEPTH,11,10,0,90,0,2R(NUMV +1)
   1ZR (NUMV+2),10.0
    CALL PLOT
              ( 15.0,0.0, -3)
  8 JP = 3
188 WRITE (4,9) HED
  9 FORMAT (1H1,9X,20A4)
    WRITE (4,10)
 10 FORMAT(1HO, 15X, 4HZ, FT, 5X, 8HC, FT/SEC)
 11 WRITE(4,12)ZR(1),CR(I)
 12 FORMAT(1H0,9X,F10.1,F12.1)
    IF (DABS(Z(I)-ZM)-.01)14,14,13
 13 I = I+1
    JP = JP+1
    IF (JP-JPM) 11.8.8
 14 READ (3,15) N. UM .FQ
 15 FORMAT(110,2F10,3)
    NNN
151 READ (3,150) ISFQ, IEFQ, NMOD, INCF
150 FORMAT (4110)
    IF (IRP, NE.1)
                   GO TO 120
    READ (3,121) IRST, IREN, IRIC, NPS, 25, ZRC .FMI
121 FORMAT (4110, 3F10.3)
    25 = ZM - 25
    ZRC = ZM - ZRC
    READ (3.122)
                   (DD(J), J= 1,NMOD)
122 FORMAT (4F10.5)
120 00 154 M=
                1.NMOD
    DO 155 L= ISFQ, IEFQ,-INCF
    IF (IVOP.NE.1)
                    GO TO 162
    FQ
102 P2 = 6,283185306
    W2 = (P2*F0)*(P2*F0)
    N = NNN
    FMOD = M
    IRLL = 0
    IF (N) 29,4,29
 29 K20 = ((W2*(CB-C(1))*(CB+C(1)))/(C(1)*C(1)*C0*CB))
    DK2= .099*K20
    K2 = -K20
 31 K2 = K2 + DK2
```

```
IF (K2-K20) 16,32,32
32 WHITE (4,33)
33 FORMAT (1HO, 13HNO MODE FOUND)
    ILFG
         = L + INCF
   IF (1VOP.Ew.1) GO TO 160
   GO TO 111
16 FLU = FLUAT(N)
   H = ZM/ DBLE(FLB)
    ZP = 0.
    J = 1
    I = 1
17 IF (ZP- Z(1+1)) 18,18,19
19 I = I+1
   GU TO 17
18 CZ = (C(I)*(Z(I+1)-ZP)+C(I+1)*(ZP-Z(I)))/(Z(I+1)-Z(I))
   CCC(J) = CZ
   6 =-(W2*(C(1)-CZ)*(C(1)+CZ))/(CZ*CZ*C(1)*C(1))
   F(J) = K2 - G
    IF (ZP-ZM) 20,21,21
20 J=J+1
   FLA = FLOAT(J -1)
   ZP = ZM+DBLE(FLA)/DBLE(FLB)
    GO TO 17
21 U(1) = 1.0
    UP(1) = (RO/RB) * DSQRT ((W2*(CB-C(1))*(CB+C(1)))/(C(1)*(C(1)*CB*CB)) 
  1-K2)
   J = 1
22 JP = 3
25 FLA =
           FLOAT(J -1)
   FLD = FLOAT(N)
    ZP = ZM+DBLE(FLA)/DBLE(FLB)
    IF (J-N-1)27,34,27
 27 IF (DABS(U(J))-UM)28,34,34
 28 J = J+1
    JP= JP+1
    H2= H+H
    DEN = 1.0 + (H2+F(J))/6.0
    U(J)= ((1.0-(H2/3.0)+F(J-1))+U(J-1)+H+UP(J-1))/DEN
    UP(J)=((1.0-(H2+F(J))/3.0)+UP(J-1)-(F(J-1)+F(J)-(H2+F(J)+F(J-1))/
   16.0) *H+U(J-1) * 0.5)/DEN
    IF (JP-JPM) 25,22,25
 34 JM = J
    CALL COUNT
195 IF (MS-M)31,35,35
 35 K2 = K2 - UK2
    DK2= DK2 / 10.0
    IF(DK2- .000001+K20 +10++(-[EX])36,36,31
 36 J = 2
    S = H*U(1)*U(1)/2.0
    52= H*U(1)*U(1)/(2.0*CCC(1)*CCC(1))
 37 IF (J-JMS) 38,39,38
 38 S = H*U(J)*U(J)+S
    S2= H+U(J)+U(J)/(CCC(J)+CCC(J)) +S2
    J = J+1
    GO TO 37
 39 S = (H+U(J)+U(J)/2.0) + S
    S2= H*U(J)*U(J)/(2.0*CCC(J)*CCC(J))
    IF (IVOP.EQ.1) GO TO 164
```

```
J = 1
 42 JP = 3
    WKITE (4,25) HED. N. KZ. UM. FQ. M
 23 FORMAT(1H1,5X,20A4,/,2X,3HN =,15,2X,4HN2 =,F15.8,2X,4HUM =,F6.1,
   12A,6HFREQ = .FG.1.2X.3HM =, [5]
WRITE(4,47) ZM.CB.RO.RB
 47 FORMAT(3X, 0HZMAX = ,F10.3,4HCB = ,F10.3,4HR0 = ,F15.8,4HRB = ,
   1F15.8)
    WRITE (4,24)
 24 FORMAT(1HU, 17X, 4HZ, FT, 10X, 1HU, 1UX, 5HDU/DZ, 11X, 4HF(Z))
 45 ZP = ZM+( FLOAT (J-1) / FLOAT (N))
    ZQ = ZM - ZP
    WRITE(4,26)ZQ,U(J),UP(J),F(J)
    IF (J-N-1)45,44,45
 45 IF (DABS(U(J))-UM)46,44,44
 40 J = J+1
    JP = JP+1
    IF (JP-JPM) 43,42,43
 44 WRITE (4,40) S
 40 FORMAT (1HU, 10X, 3HS = ,F15.5)
164 UMAX = 0.0
    NM = N + 1
    DO 104 K= 1. NM
    IF ( DABS (U(K)) - UMAX) 104,104,103
103 UMAX = DABS(U(K) )
104 CONTINUE
    00 105
             K= 1. NM
105 UU(K) = U(K)/UMAX
    DO 106 K= 1. NM
106 \ ZZP(K) = ZM*(FLOAT(K-1)/FLOAT(N))
    GAM = DSQRT(K20 - K2)
    BA = (RO+C(1))/(2.0+RB+CB+GAM+5 )
    WRITE(4,41) BA.GAM
 41 FORMAT(1HU, 10X, 5HB/A = ,F15.5,5x,7HGAMMA = ,F15.5 )
    SS= R0+5/(UMAX+UMAX)+R0+ R0+U(1)+U(1)/(UMAX+UMAX+2.0+GAM+RB)
    SSS= RO+S2/(UMAX+UMAX)
                                               RO+RO+U(1)+U(1)/(UMAX+UMAX
   1+2.0+GAM+RB+CB+CB)
    IF (IVOP.EQ.1) GO TO 153
    E = DEXP(-GAM+h)
    ZP = 0.0
    V = 1.0
    NN
    ZPP(1) = 0.0
    VV(1) = UU(1)
    WRITE (4,23) HED, N. KZ, UM, FQ, M
    WRITE(4,47) ZM,CB,RO,RB
    WRITE (4,48)
 48 FORMAT (1HO, 17X, 4HZ, FT, 10X, 1HU )
 49 WRITE (4,26) ZP. V
 26 FORMAT(1H0,F22.2,F13,3,F13,3,F16.5)
 50 V = V*E
    NN = NN
    AN = NN + 1
AN = NN + 1
             = ZP -
    ZPP (NN)
    ZP = ZP-H
    IF (ZPP(NN) + 50.0)
                                    110, 110, 49
113 CALL PLOT ( 5.0.0.0, -3)
DO 184 NINX = 1, NN
```

```
184 ZPP(NINX) = ZM - ZPP(NINX)
        NINV = N + 1
        DO 183
                            NINW = 1. NINV
183 ZZP(NINW) = ZM - ZZP(NINW)
         VV(NN +1)
                               = -1.0
         (S+ MM) VV
                               =
                                       U.5
         ZPP(NN +1) = 200.0+FSC
         ZFP(NN +2) = -20.0*FSC
         ZZP(N +2) = 200.0.FSC
         22P(N +3)
                                = -20.0+FSC
        UU(N+2) = -1.0

UU(N+3) = 0.5
         CALL AXIS (0.0,0.0, 9HAMPLITUDE: 9.4.0,0.0,UU(N+2).UU(N+3).10.0)
         CALL AXIS (0.0,0,0,16HWATER DEPTH (FT),16,10.0,90.0.ZZP(N+2),
           ZZP(N +3).10.0)
        CALL LINE (UU. 22P. N+1, 1.0.0)
         CALL LINE (VV. ZPP. NN. 1.0.0 )
         CALL LINE (ZBF.ZBT,2,1,0,0)
         CALL SYMBOL (10.25, ZMB, 0.14, 6HBOTTOM, 0.0,6)
         CALL SYMBOL (1.3,9.50,0.14,9HAMPLITUDE,0.0,9)
         CALL SYMBOL (1.7.9.25.0.10.6HVERSUS, 0.0.6)
         CALL SYMBOL (1.6,9.00,0.14,5HDEPTH,0.0,5)
         CALL SYMBOL (0.8,8.75,0.14,19HFREQUENCY
                                                                                                              HZ.0.0.19)
         CALL NUMBER (2.2,8.75,0.14,FQ,0.0,-1)
         CALL SYMBOL (1.4.8.50,0.14.4HMODE.0.0.4)
         CALL NUMBER (2.1,8.50,0.14,FMOD, U.U,-1)
         NUM = NUM +1
         XMP(1) = 0.0

ZMP(1) = 0.0
153 XMP(1)
         NM = N +1
DO 170 K= 1.NN
         IF(F(1).67.0.0)
                                                60 TO 179
         IF (F(K).GT.0.0)
                                                  GO TO 171
170 IRTB = K
171 COS2(IRTB +1) = F(1RTB +1) * CCC(IRTB +1) * CCC(IRTB +1)/W2
                       CCC(IRTO +1)/DSQRT(1.0 - COS2(IRTB +1))
         ZMP(2) = H*(CV - CCC(1RTB +1))/(CCC(1RTB)-CCC(1RTB +1))
         XMP(2) = (ZMP(2) - ZMP(1))*(CCC(1RTb +1) + CV)/(CV*(DSQRT(COS2))
       1 (IRTB +1))))
         ZMP(1) = FLOAT(IRTb)*H - ZMP(2)
         ZMP(2) = ZMP(1) + ZMP(2)
         NM = NM -INTB +1
         DO 172 K = 3, NM
         TH1 = 90.0
         KO = IRTB -1 +K
        COS2(KO-1) = F(KO -1)+CCC(KO -1)+CCC(KO -1)/#2
         COS2(KO)=F(KO)*CCC(KO)*CCC(KO)/%2
         TH2 = (ACOS(SQRT(COS2(NM +IRTB -1))))+57.2958
         IF (CCC (KO) .GE.CV)
                                                 GO TO 142
        XMP(K) = XMP(K -1) + H+(CCC(KO -1) + CCC(KO))/(CV+(DSQKT(COS2(KO-1) + CCC(KO)))/(CV+(DSQKT(COS2(KO-1) + CCC(KO)))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(CCC(KO))/(C
      1)) + USQRT(COS2(KO))))
                                (KO -1)+H
172 ZMP(K) =
         N = NM -1
         60 TO 173
179 CO52(1) = ABS(F(1))+CCC(1)+CCC(1)/w2
         CV = CCC(1)/DSQRT(1.0 - COS2(1))
         DO 140 K= 2.NM
        CO52(K -1) = ABS(F(K -1)) +CCC(K -1)+CCC(K -1)/#2
```

```
COS2(K) = ABS(F(K))+CCC(K)+CCC(K)/W2
    TH1 =(ACOS(SQRT(COS2(1))))+57,2958
    THE = (ACOS (SQRT (COS2 (NM)))) +57.2958
    IF( CCC(K).GE.CV) GO TO 142
    XMP(K) = XMP(K-1) + H*(CCC(K-1) + CCC(K))/(CV*(DSQRT(COS2(K-1))+
   1 DSQRT(COS2(K))))
140 \text{ ZMP(K)} = (K-1)*H
           K= 1.is
173 DO 141
    XMP(NM + K) = 2.0 + XMP(NM) - XMP(NM - K)
141 ZMP(NM +K) = ZMP(NM -K)
    GO TO 143
142 ZMP(K) = ZMP(K-1) + H*(CV - CCC(K-1))/(CCC(K) - CCC(K-1))
    TH2 = 90.0
    XMP(K) = XMP(K-1) + (ZMP(K) - ZMP(K-1)) + (CCC(K-1) + CV)/(CV+(CV+1))
   1 DSQRT(CO52(K -1))))
    N = K -1
    NM =
    DO 144 K= 1.14
    XMP(N+1+K) = 2.0*XMP(N+1) - XMP(N+1-K)
144 \text{ ZMP}(NM + K) = \text{ZMP}(NM - K)
143 \times MP(2*NM) = 0.0
182 \times MP(2*NM +1) = 1000.0
    NI2Z = 2*NM -1
    DO 186 NINZ = 1, NIZZ
186 ZMP(NINZ) = ZM - ZMP(NINZ)
    ZMP(2*NM) = 200.0*FSC
    ZMP(2*NM +1) = -20.0*FSC
    WRITE (4,145) TH1, TH2
IF (IVOP.EQ.1) GO TO
                    GO TO 157
145 FORMAT (2F10.3)
    CALL PLOT (15.0,0.0,-3)
    CALL LINE (XMP, ZMP, NM +N, 1, 0, 0)
    CALL LINE (ZBF, ZBT, 2, 1, 0, 0)
    CALL SYMBOL (10.25, ZMB, 0.14, 6HBOTTOM, U.O.6)
    CALL AXIS (0.0,0.0,10HRANGE (FT),10,12.0,0.0,XMP(2*NM)
   1XMP(2*NM +1),10.0)
    CALL AXIS (0.0.0.0.16H
                                  DEPTH (FT),16,10.0,90.0,ZMP(2*NM),
   1 ZMP(2+NM +1),10.0 )
    CALL SYMBOL (5.0,9.50,0.14,14HRAY EQUIVALENT,0.0,14)
    CALL SYMBOL (5.0,9.25,0.14,19HFREQUENCY
                                                     HZ.0.0.19)
    CALL NUMBER (6.4,9.25,0.14,FQ.0.0,-1)
    CALL SYMBOL (5.5,9.00,0.14,4HMODE,0.0,4)
    CALL NUMBER (6.2,9.00,0.14,FMOD,0.0,-1)
    CALL PLOT (15.0,0.0,-3)
    IF (IVOP.NE.1)
                      GU TO 154
157 T1(L) = TH1
    T2(L) = TH2
    FMH = SQRT(P2*FQ /(30.48*CV) )
                            RO/(FMH+2.0+(SS) )
    PM(L) = SQRT(P2)*
    GVEL(L) = SS/(CV*SSS)
    FQP(L) = L
    WRITE ( 4,166) PM(L) , FMH, SS , GVEL(L)
166 FORMAT (4F10.3)
    IF (IRP.EQ.1) PM(M) = PM(L)
    FMR(M) = P2*FQ/CV
    IZS = ZS*FL8/ZM
                       +1.0
    IZR =ZRC+FLB/ZM
                       +1.0
    USK(M) = U(IZS)/UMAX
```

```
URR(M) = U(IZR)/UMAX
   PMM(M) = PM(M) *USR(M) *URR(M)/RO
155 PVLL(L) = CV
    IF (IRP.EQ.1) 60 TO 154
         = (ISFG - IEFG)/INCF +1
160 IUF
   LIFO = IDF -1
    DO 161 LLL= 1. IDF
                 -1) * INCF
    ILL = (LLL
   FQP(LLL)
             = FOP(IEFQ+ILL)
    GVEL (LLL) =
                 GVEL (IEFQ+ILL)
               T1(IEFQ+ILL)
    T1(LLL) =
            = T2(IEFQ+ILL)
    T2(LLL)
   PM(LLL) = PM(IEFQ + ILL)
161 PVEL(LLL) = PVEL(IEFQ+ILL)
    WRITE (4,163)
                  (PVEL(J), GVEL(J), FQP(J), PM(J), J= 1, IDF)
163 FORMAT (4F10.3)
   FQP(LIFQ +2)
                    0.0
   FQP(LIFQ +3) = ISFQ/10
   PVEL(LIFQ +2)
                  = 3500.0
   PVEL(LIFQ +3)
                      250.0
                   =
    GVEL (LIFQ +2)
                   =
                      3500.0
                  =
   GVEL(LIFQ +3)
                      250.0
   PM(LIFQ +2)
                 = 0.0
   PM(LIFQ +3)
                 = 0.1
    CALL PLOT (15.0,0.0,-3)
   CALL LINE (FQP, PVEL, LIFQ +1,1,10,14)
    CALL LINE (FQP, GVEL, LIFQ +1,1,10,28)
    CALL LINE (FOP, PM, LIFO +1,1,10,4)
   CALL AXIS (0.0,0.0,14HFREQUENCY (HZ),14,10.0,0.0,FQP(LIFQ +2),
   1 FQP(LIFQ +3),10.0)
   CALL AXIS (0.0,0,0,27HSOUND VELOCITY (FT PER SEC),27,10.0,90.0,
     PVEL (LIFQ +2), PVEL(LIFQ +3), 10.0)
    CALL AXIS(10.000.0,18HEXITATION PRESSURE,-18,10.,90.0,PM(LIFQ +2),
   1 PM(LIFO +3) . 10.0)
    CALL SYMBOL(2.4,9.50,0.14,38HSOUND VELOCITY AND EXCITATION PRESSUR
   1E,0.0,38)
    CALL SYMBOL (4.7,9.25.0.10.6HVERSUS,0.0.6)
   CALL SYMBOL (4.4,9.00,0.14,9HFREGUENCY,0.0,9)
   CALL SYMBOL (4.5,8.75,0.14,4HMODE,0.0,4)
   CALL NUMBER (5.2,8.75,0.14,FMOD,0.0,-1)
   CALL SYMBOL (4.7,8.50,0.10,14HPHASE VELOCITY,0.0,14)
   CALL SYMBOL (4.2,8.50,0.10,14,0.0,-1)
   CALL SYMBOL (4.7,8.25,0.10,14HGROUP VELOCITY,0.0,14)
   CALL SYMBOL (4.2,8.25,0.10,28,0.0,-1)
   CALL SYMBOL(4.7,8.00,0.10,19HEXCITATION PRESSURE.0.0,19)
   CALL SYMBOL (4.2,8.00,0.10,4,0.0,-1)
     T1(LIFG
             +2) = 90.0
    T1(LIFQ +3) = -10.0
    T2(LIFQ +2)
                 = 90.0
     T2(LIFQ
             +3)
                  = -10.0
   CALL PLOT (15.0,0.0,-3)
   CALL LINE (FQP, T1, LIFQ +1,1,10,4)
   CALL LINE (FQP, T2, LIFG +1,1,10,5)
   CALL AXIS (0.0.0.0,14HFREQUENCY (HZ),-14,10..0.0,Fup(LIFQ +2),
  1 FQP(LIFQ +3),10.0)
   CALL AXIS (0.9.0.0,28HANGLE OF INCIDENCE (DEGREES):28, 9.0.90.0.
     T1(LIFQ +2), T1(LIFG +3),10.0)
   CALL SYMBOL (3.7,9.50,0.14,18HANGLE OF INCIDENCE,0.0.18)
```

```
CALL SYMBOL (4.7,9.25.0.10.6HVERSUS.0.0.6)
    CALL SYMBUL (4.4,9.00,0.14,9HFREQUENCY,0.0,9)
    CALL SYMBOL (4.5,8.75,0.14,4HMODE,0.0,4)
    CALL NUMBER (5.2,8.75,0.14,FMOD.0.0,-1)
    CALL SYMBOL (4.5,8.50.0.10.25HBOTTOM ANGLE OF INCIDENCE.0.0.25)
    CALL SYMBOL (4.0,8.50,0.10,4,0.0,-1)
    CALL SYMBUL (4.5,8.25,0.10,26HSURFACE ANGLE OF INCIDENCE,0.0,26)
    CALL SYMBOL (4.0,8,25,0.10,5,0.0,-1)
154 CALL PLOT (15.0,0.0,-3)
    IF (IRP.NE.1) 60 TO 111
123 DO 124 IP= 1.NPS
    READ (3,125)
125 FORMAT (110)
    READ (3,126)
                  (MUS(J), J=1,NMS)
126 FORMAT (6110)
    DO 131 IR = IRST, IREN, IRIC
    IREO = (IR -IRST)/IRIC +1
    PCT(IREO) = 0.0
131 PST (IREO) =
                  U.0
    DO 127 IG= 1,NMS
    M= MOS(IQ)
    DO 129 IR = IRST, IREN, IRIC
    RR = IR
    IREO = (IR -IRST)/IRIC +1
    DDT(M) = 10.0**(-DD(M)*RR/20.0)
    PST(IREO) = PST(IREO)+PMM(M)+DDT(M)
                                                  *SIN(FMR(M)*RR-P2/8.0)
                  PCT(IREO)+PMM(M)+DDT(M)
    PCT(IREO)=
                                                  *COS(FMR(M)*RR-P2/8.0)
129 CONTINUE
127 CONTINUE
    DO 132 IR = IRST, IREN, IRIC
    RR
       = IR
    IREO = (IR -IRST)/IRIC +1
    PPT(IREO) = SQRT(PCT(IREO) + PCT(IREO) + PST(IREO) +PST(IREO)) +RO/
   150RT (RR/3.0)
    PPT (IREO
                   ) =-20.0*ALOG10(PPT(IREO))
132 RP(IREO
                  ) = FLOAT(IR)/6000.0
WRITE (4,128) (PPT(J), J= 1, IREO
128 FORMAT (10F10,5)
    RP(IREO +1)
    RP(IREO +2)
                 = FM1
    PPT(IREO +1)
                 =
                     30.0
    PPT(IREO +2)
                  = 10.0
    ZS = ZM - ZS
    ZRC = ZM - ZRC
    CALL LINE (RP.PPT. IREO. 1. 10.4)
    CALL AXIS(0.0,0.0,13HRANGE (MILES),13,20.0,0.0,RP(IREO +1),
   1 RP(IREO +2),10.0)
    CALL AXIS(0.0,0,0,21HPROPAGATION LOSS (UB),21,10.0,90.0.
   1 PPT(IREO +1), PPT(IREO +2), 10.0)
    CALL SYMBOL (8.9,9.50,0.14,16HPROPAGATION LUSS, U. 0,16)
    CALL SYMBOL (9.7,9.25,0.10,6HVERSUS,0.0,6)
    CALL SYMBOL (9.7,9.00,0.14,5HRANGE,0.0,5)
    CALL SYMBOL (8.9, 8.75, 0.14, 18HFREQUENCY
                                                   HZ, 0.0.18)
    CALL NUMBER (10.3.8.75..14.FQ.0.0.-1)
    CALL SYMBOL (8.6,8.50,0.14,20HSOURCE DEPTH
                                                     FT.0.0.20)
    CALL NUMBER (10.5.8.50,0.14, ZS,0.0,-1)
    CALL SYMBOL (8.6,8.25,0.14,22HRECEIVER DEPTH
                                                       FT.0.0.22)
    CALL NUMBER (10.6,8,25,0.14,2RC,0.0,-1)
```

CALL SYMBOL (8.6,8.0,0.14,5HMODES,0.0,5)
DO 187 J= 1,NMS
FUS(J) = MDS(J)

187 CALL NUMBER (9.1 +0.5*J,8.0,0.14,FUS(J),0.0,-1)
CALL PLOT (15.0,0.0,-3)

124 CONTINUE
CALL PLOT (15.0,0.0,-3)
111 CALL PLOT (15.0,0.0,-3)
END

SUBROUTINE COUNT DIMENSION U(500) DUBLE PRECISION U COMMON MS,JM+U COMMON JMS MS=0 J=1 15=1 JMS=1 5 IF (U(J)) 1,2,3 3 IS1=IS IS=1 7 IF (IS-IS1) 4,2,4 4 MS=MS+1 JMS=J 2 J=J+1 IF (J-JM-1) 5,6,5 1 IS1=IS IS=0 60 TO 7 6 RETURN END

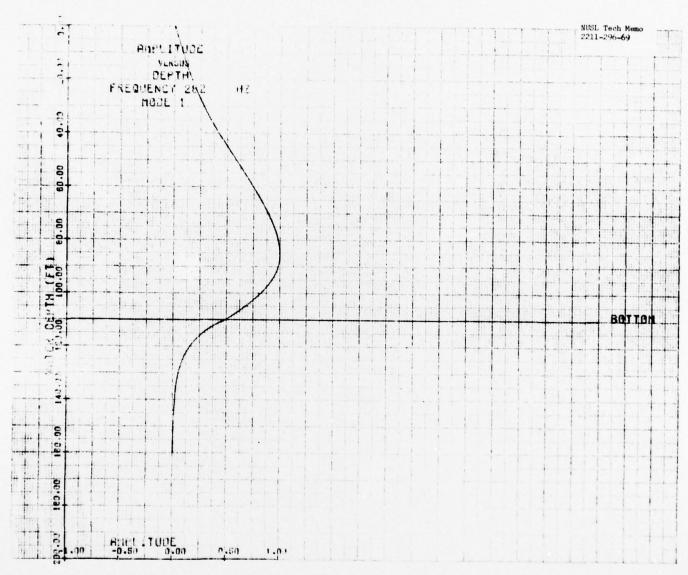
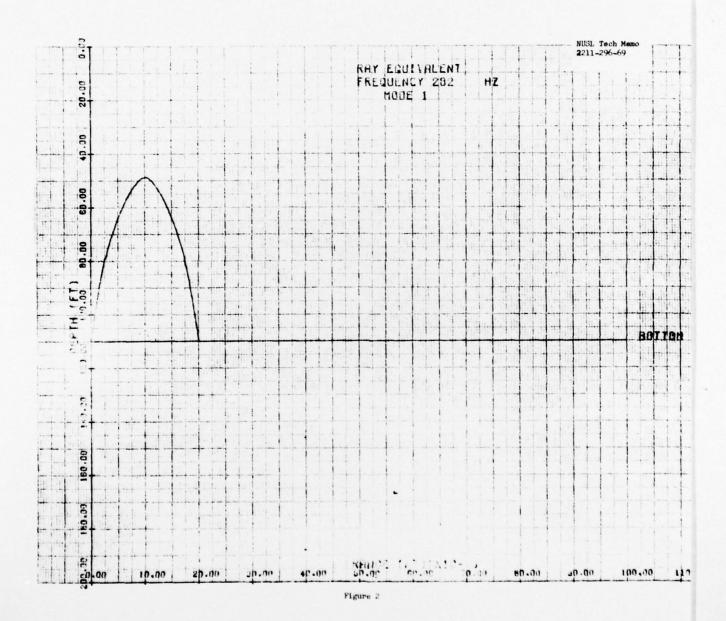
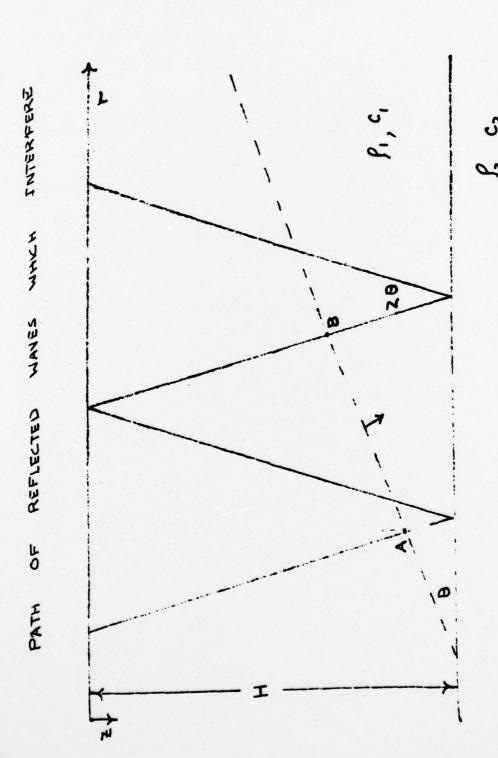


Figure 1





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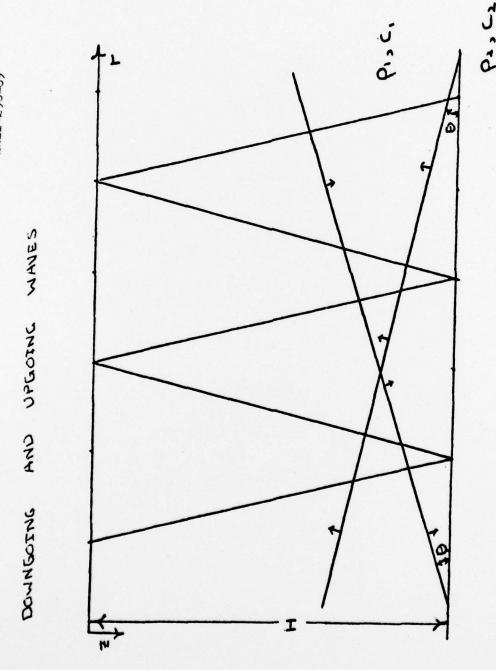


Figure 4

Figure 5

Figure 6

Pic,

7 · 1

Paca

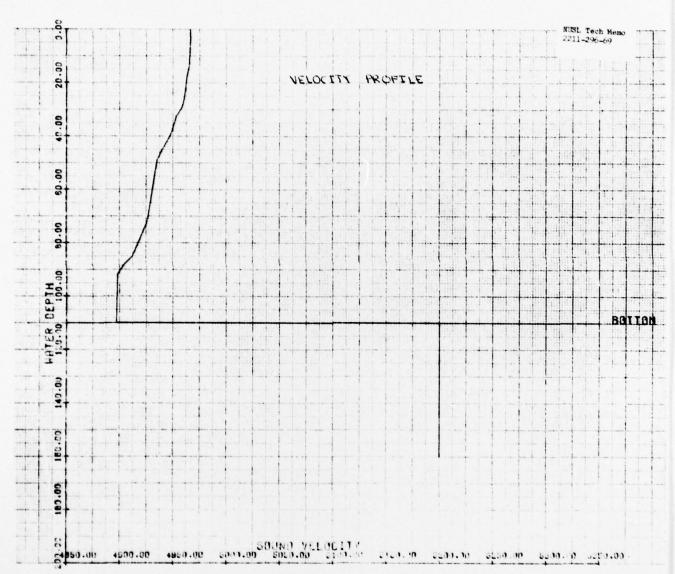


Figure 7

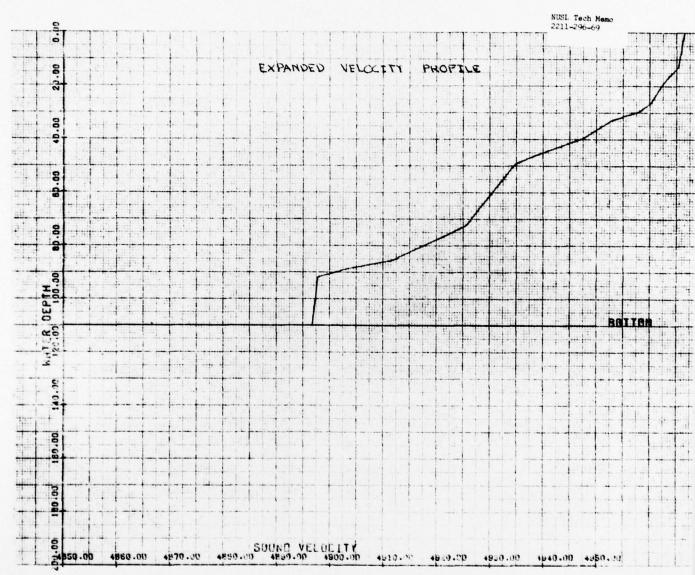


Figure 8

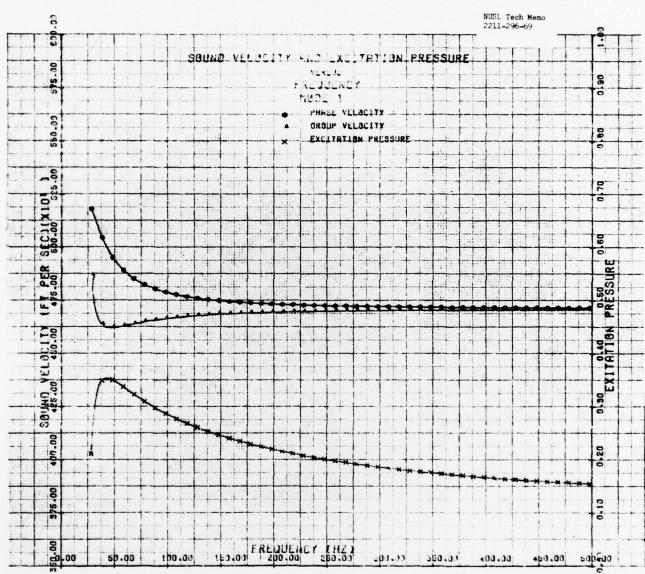


Figure 9

